## PHASE EQUILIBRIA

a free energy, too. It seems therefore not unreasonable to discuss critical mixing in terms of the critical conditions derived from the Flory-Huggins theory ( $\chi_c = 0.5$  for polymer of infinite molecular weight), and to expect  $\chi_c$  to be given approximately by the solubility parameter term.

Assuming the volume of change of mixing not to be excessive, the solubility parameter for a gas can be calculated by substituting its energy of compression,  $\Delta E_1$ , for the energy of vaporization<sup>1</sup> of the standard treatment. The solubility parameter for the solvent,  $\delta_1$ , is then taken to be the square root of the cohesive energy density,  $\Delta E_1/V_1$ , where  $V_1$  is the molar volume of the solvent. Table II lists the solubility parameters at the UCSP, calculated by means of a reduced variable correlation.<sup>16</sup>  $\delta_1$  is seen to vary with temperature, but to be nearly constant at a given temperature for all alkanes studied, although a slight drop with the size of the solvent molecule seems indicated. If one uses the value of Allen et al.<sup>17</sup> for an amorphous linear polyethylene ( $\delta_2$  is 8.37 cal.<sup>1/2</sup> cc.<sup>-1/2</sup> at a density of 0.855 g. cc.<sup>-1</sup>), and allows  $\delta_2$  to vary as  $a^{1/2}/V_2^{-1}$  (van der Waals fluid behavior), one obtains values of  $\chi$  in the range of 0.4-0.8. Positive deviations from 0.5 increase with the size of the solvent molecule and with temperature. The data are, therefore, not quantitatively consistent with the approach outlined. A very rough estimate of the UCSP from the thermodynamic properties of the components is, however, possible. In the *n*-alkane-polyethylene systems investigated, furthermore, the UCSP for a given solvent at a given temperature is evidently calculable with reasonable accuracy from that of another by assuming critical mixing to occur at a fixed value of  $\delta_1$ . Note, however, that at least equally successful a calculation could be made in terms of reduced densities (Table II).

The critical locus of binary alkane systems whose components differ only moderately in size is a continuous unbroken line joining the critical points of the pure components. Katz and Rzasa<sup>5</sup> in a detailed optical study of methane with an oil fraction containing mostly C<sub>20</sub> paraffin, have shown that, as the size difference between the components increases, the maximum pressure on the critical locus rises and is shifted toward the component of low molecular weight. Freeman and Rowlinson,<sup>3</sup> however, found that solutions of hydrocarbon polymers in hydrocarbon solvents, upon heating under their own vapor pressures, break up into two liquid phases at a LCST which can be well below the critical point of the solvent. This LCST must also be the lower critical end point (LCEP) of the critical locus which, if closed along the pressure axis, must change gradually from a liquid-liquid to a gas-liquid boundary.<sup>4</sup> This lack of sharp distinction between liquid and gaseous solvents is demonstrated in this study which shows sections of the critical locus of polyethylene with solvents which are above, below, and close to their critical temperatures. The slope of the critical locus at a given temperature differs in sign and magnitude (Table II, Fig. 5); it is close to zero, but slightly negative, with propane just above its own critical point of 97°C. This suggests that the critical